

# Interpreting Deep Sports Analytics: Valuing Actions and Players in the NHL

Guiliang Liu, Wang Zhu, Oliver Schulte  
Machine Learning Lab

The logo for the European Conference on Machine Learning (ECML) and the Pot Knowledge Discovery and Data Mining (PKDD) conference. It features the text 'ECML PKDD' in a large, bold, green font, with 'Dublin, Ireland' in a smaller green font below it. The background is a green-tinted aerial view of a city.A green rectangular box containing the text '10-14 SEPT 2018' in white, bold, sans-serif font. The background is a green-tinted aerial view of a city.

# Problem

Understand the Deep Reinforcement Learning (DRL)  
Model in National Hockey League (NHL)



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# DRL Model: Previous Work

Liu and Schulte IJCAI 2018

# Dataset

- *Game events* and *player actions* for the 2015-2016 NHL season.
- Augment the data with derived features (red lines).

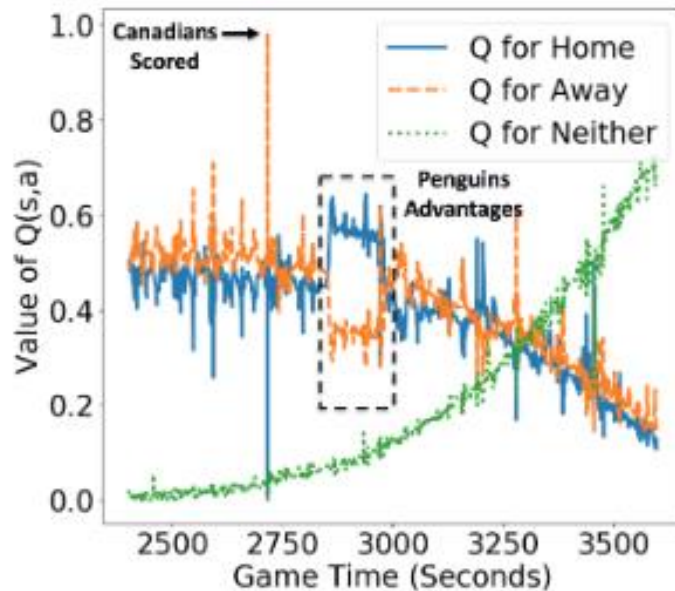
Table 3: Complete Feature List. Values for the feature Manpower are EV=Even Strength, SH=Short Handed, PP=Power Play.

Name	Type	Range
X Coordinate of Puck	Continuous	[-100, 100]
Y Coordinate of Puck	Continuous	[-42.5, 42.5]
<u>Velocity of Puck</u>	Continuous	(-inf, +inf)
<u>Time Remaining</u>	Continuous	[0, 3600]
Score Differential	Discrete	(-inf, +inf)
Manpower	Discrete	{EV, SH, PP}
<u>Event Duration</u>	Continuous	[0, +inf)
Action Outcome	Discrete	{successful, failure}
<u>Angle between puck and goal</u>	Continuous	[-3.14, 3.14]
Home/Away Team	Discrete	{Home, Away}

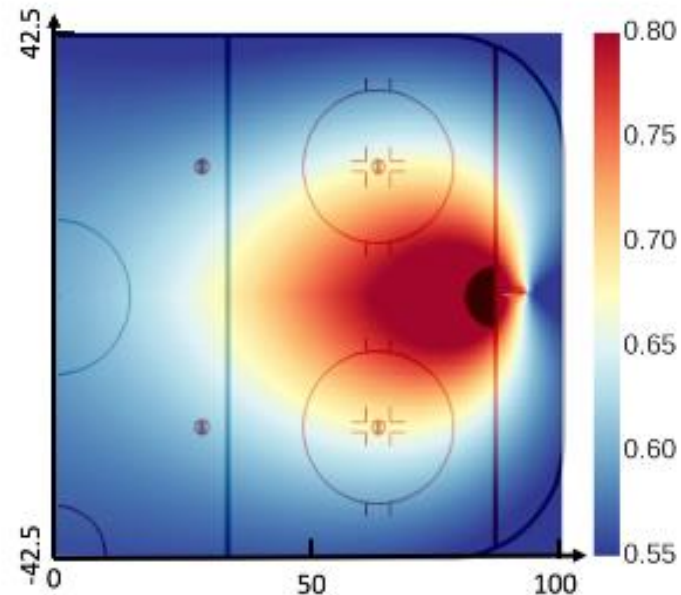
- Divide NHL games into **goal-scoring episodes** that
  - Begin at the beginning of the game, or after a goal.
  - Terminate with a goal, or the end of the game.

# DRL Model

- Estimate chance that team scores the next goal given current match state and action =  $Q_{team}(s, a)$ .
- Recurrent network with dynamic trace length LSTM.



Temporal Projection: evolution of scoring probabilities for the next goal



Spatial Projection (for shot): The probability that the home team scores the next goal after taking a shot at a rink location

# Goal Impact Metric

- ***Impact***( $s_t, a_t$ ) measures the quality of action  $a_t$  by how much it changes the expected return of a player's team.

$$impact^{team}(s_t, a_t) = \frac{Q^{team}(s_t, a_t) - Q^{team}(s_{t-1}, a_{t-1})}{\text{Difference of consecutive Q values}}$$

Difference of consecutive Q values

- Define **Goal Impact Metric (GIM)** of player  $i$  by the total impact of a player in entire game season dataset  $D$ .

$$GIM^i(D) = \sum_{s,a} n_D^i(s, a) \times impact^{team_i}(s, a)$$

# Goal Impact Metric

- The **Impact** metric passes “eye test”.
- Correlates strongly with goals, points, salary, etc. in NHL.
- Consistent between and within seasons.
- All actions including **defensive** and **offensive** actions.

Table 4: 2015-2016 Top-10 Player Impact Scores

Name	GIM	Assists	Goals	Points	+/-	Age	Team	Salary
Taylor Hall	96.40	39	26	65	-4	24	EDM	\$6,000,000
Joe Pavelski	94.56	40	38	78	25	31	SJS	\$6,000,000
Johnny Gaudreau	94.51	48	30	78	4	22	CGK	\$925,000
Anze Kopitar	94.10	49	25	74	34	28	LAK	\$7,700,000
Erik Karlsson	92.41	66	16	82	-2	25	OTT	\$7,000,000
Patrice Bergeron	92.06	36	32	68	12	30	BOS	\$8,750,000
Mark Scheifele	90.67	32	29	61	16	23	WPG	\$832,500
Sidney Crosby	90.21	49	36	85	19	28	PIT	\$12,000,000
Claude Giroux	89.64	45	22	67	-8	28	PHI	\$9,000,000
Dustin Byfuglien	89.46	34	19	53	4	31	WPG	\$6,000,000

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# Interpreting the DRL Model



# Model

## Mimic Learning Framework for **General Model**:

- Mimicking Q functions and impact separately.
- History Window of last 10 observations.
- A Multi-variate Regression Tree (MRT) trained with CART method.

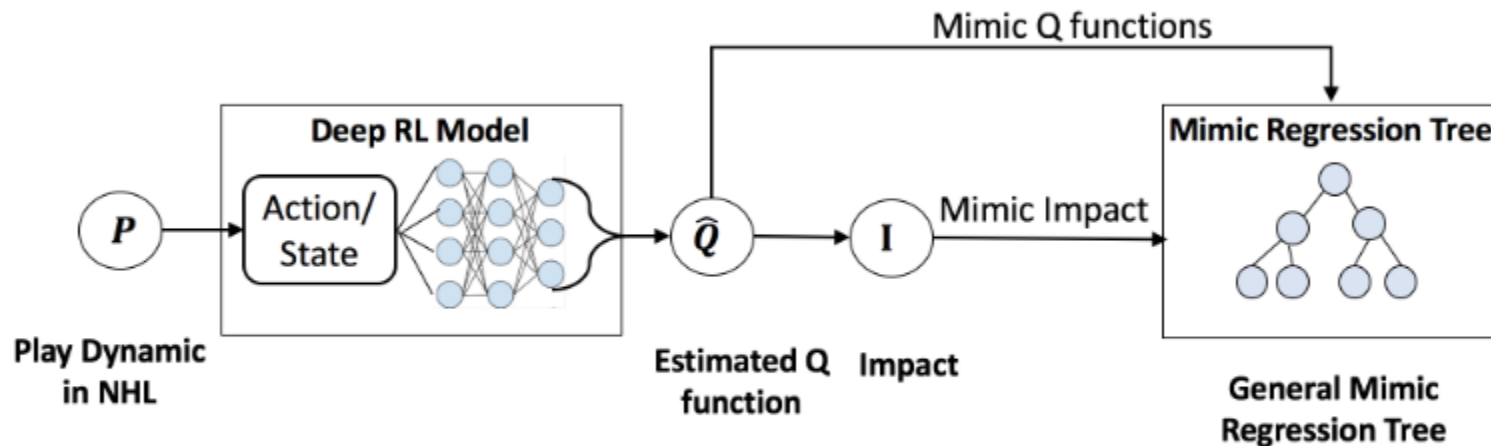
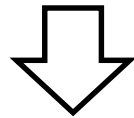


Fig. 3: Interpretable Mimic Learning Framework

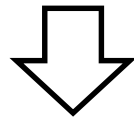
# Model

## Player Specific Model:

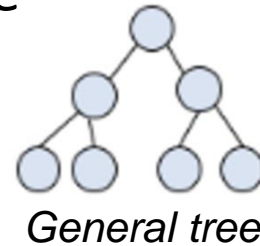
- Inherit the tree structure of the *general model*.



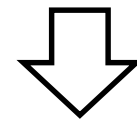
- Use the target player data to prune the *general model*.



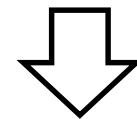
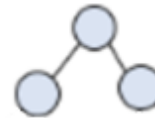
- Use the same player data to expand the tree.



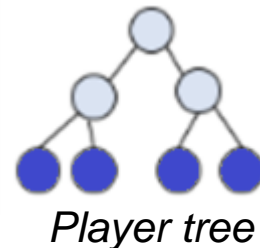
*initialize*



*prune*



*expand*



e.g. Sidney Crosby

# Model

## Mean Sample Leaf (MSL):

- Control the minimum number of samples at each leaf node.
- Satisfactory performance when **MSL = 20**.

Table 5: Performance of General Mimic Regression Tree (RT) with different Minimum Samples in each Leaf node (MSL). We apply ten-fold cross validation and report the regression result with format: Mean Square Error (Variance)

model	Q_home	Q_away	Q_end	Impact
RT-MSL1	3.35E-04 (1.43E-09)	3.21E-04(1.26E-09)	1.74E-04(2.18E-09)	1.33E-03(5.43E-09)
RT-MSL5	2.59E-04(1.07E-09)	2.51E-04(0.89E-09)	1.35E-04(1.87E-10)	9.84E-04(2.72E-09)
RT-MSL10	2.38E-04(1.02E-09)	2.30E-04(0.89E-09)	1.25E-04(2.30E-10)	8.66E-04(2.17E-09)
<b>RT-MSL20</b>	<b>2.31E-04(0.92E-09)</b>	<b>2.22E-04(0.82E-09)</b>	<b>1.23E-04(2.05E-10)</b>	7.92E-04(1.45E-09)
RT-MSL30	2.35E-04(0.98E-09)	2.27E-04(0.85E-09)	1.27E-04(2.32E-10)	7.67E-04(1.16E-09)
RT-MSL40	2.39E-04(0.96E-09)	2.30E-04(0.85E-09)	1.29E-04(2.19E-10)	<b>7.58E-04(1.10E-09)</b>

# Feature Importance

Rank feature by average variance reduction:

- Find the top 10 important features using *general model*.
- The impact function recognizes **shooting, successful** actions.
- History Window is necessary.

Table 6: Top 10 features for Q values (left) and Impact (right). The notation  $T - n : f$  indicates that a feature occurs  $n$  time steps before the current time.

Feature Name	Frequency	Importance	Feature Name	Frequency	Importance
T: Time Remaining	12,524	0.817431	T: Goal	1	0.160595
T-1: Manpower	93	0.070196	T: Shot-on-Goal	1	0.099482
T-1: Team Identifier	57	0.020504	T: X Coordinate	7,142	0.077410
T: Manpower	346	0.017306	T: X Velocity	8,087	0.041903
T: Shot	31	0.011159	T-1: X Coordinate	3,591	0.041847
T: Score Differential	3,229	0.009568	T: Angle to Goal	7,525	0.041607
T: X Coordinate	11,797	0.006968	T: Time Remaining	8,669	0.036289
T-1: X Coordinate	3,406	0.006963	T: Duration	7,411	0.028831
T-2: Manpower	82	0.005045	T: Home/Away Team	378	0.027177
T: Home/Away Team	135	0.003755	T: Y Coordinate	6,890	0.027597

# Partial Dependence

Partial Dependence plot:

- Use *general model* to interpret Q functions and impact.
- Select Time Remaining, X Coordinate and X Velocity to visualize.

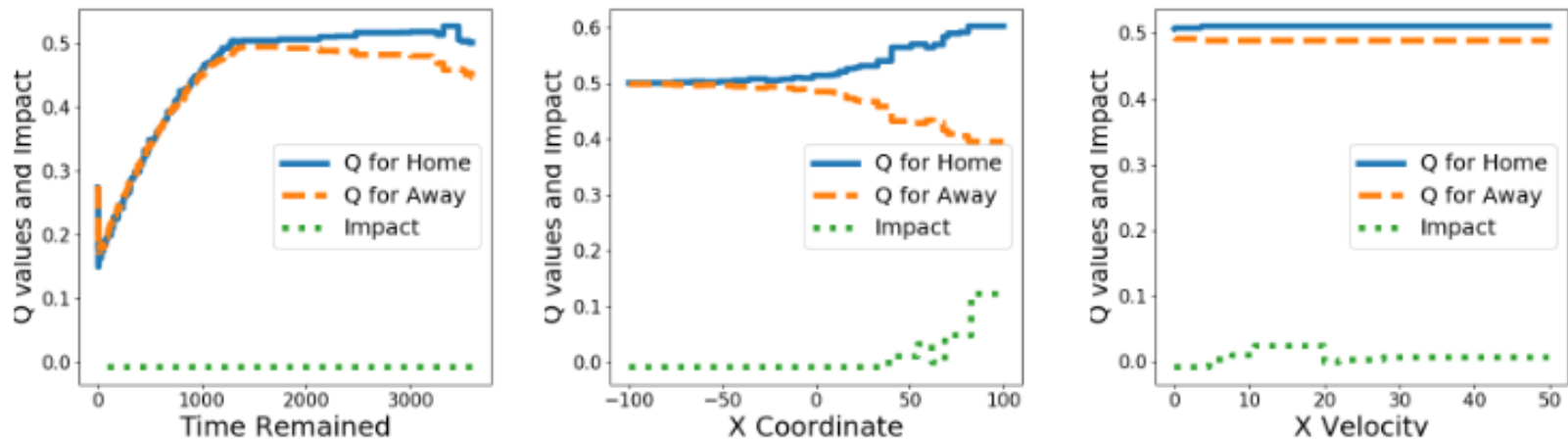


Fig. 4: Partial Dependence Plot for Time Remaining (left), X Coordinate (middle) and X Velocity (right)

# Exceptional Players

Find the most unusual players:

- Use *player specific model* to compare the whole dataset (general data) and player specific data.

Table 7: Exceptional Players Based on Tree Discretization

Player	Q_home	Q_away	Q_end	Impact
Taylor Hall	1.80E-04	2.49E-04	2.28E-04	6.66E-05
Joe Pavelski	<b>4.64E-04</b>	<b>2.90E-04</b>	<b>3.04E-04</b>	1.09E-04
Johnny Gaudreau	2.12E-04	1.96E-04	1.43E-04	6.77E-05
Anze Kopitar	2.58E-04	2.00E-04	2.43E-04	8.28E-05
Erik Karlsson	2.97E-04	1.89E-04	1.86E-04	<b>2.00E-04</b>

- Joe Pavelski scored the most in the 2015-2016 game season.
- Erik Karlsson had the most points (goal+assists).

# Thank You!



For more information:

Poster: #xxx

Homepage: <http://www.galenliu.com/>

# Exceptional Players

How to find the most unusual player:

- Focus on top players
- For each *player specific model*:
  - For each leaf in the tree
    - There is an original value (e.g.  $I_l^P$ )
    - Learn a value based on the whole dataset ( $I_l$ )
    - Weight by the percentage of cases that get to the leaf ( $n_l/n_D$ )
    - Sum over squared differences  $n_l/n_D (I_l^P - I_l)^2$

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